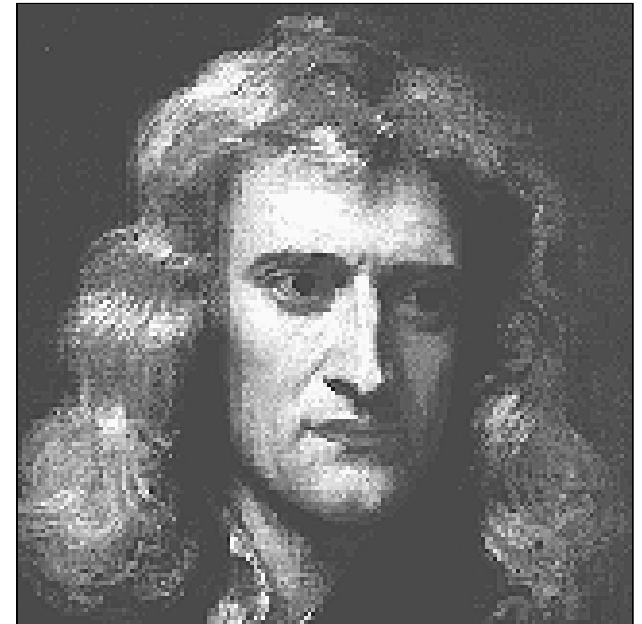


- hydrostatic pressure variation in the vertical
- *horizontal* pressure gradients – their relation to temperature gradients
- “height gradients” correspond to pressure gradients
- range of scales of atmospheric motion
- on the large scale, there exists a theoretical relationship between wind speed in the free atmosphere and the height gradient



Sir Isaac Newton  
1642 - 1727

## The hydrostatic equation (Sec. 4-3, p112)

Gives the change in pressure ( $\Delta p$ ) associated with an increase ( $\Delta z$ ) in height

$$\frac{\Delta p}{\Delta z} = - \rho g \quad \left[ \text{Pa m}^{-1} \right]$$

$\rho$  = air density  $\quad [ \text{kg m}^{-3} ]$  (approximately 1, near ground)  
 $g$  = grav. accel'n = 9.81  $[ \text{m s}^{-2} ]$  (approximately 10)

**Thus:** near ground, pressure increases by an amount  $\Delta p = - 10 \text{ Pa}$  for each 1 m increase in height

100 Pa (= 1 hPa)      per 10m  
100 hPa                per 1 km

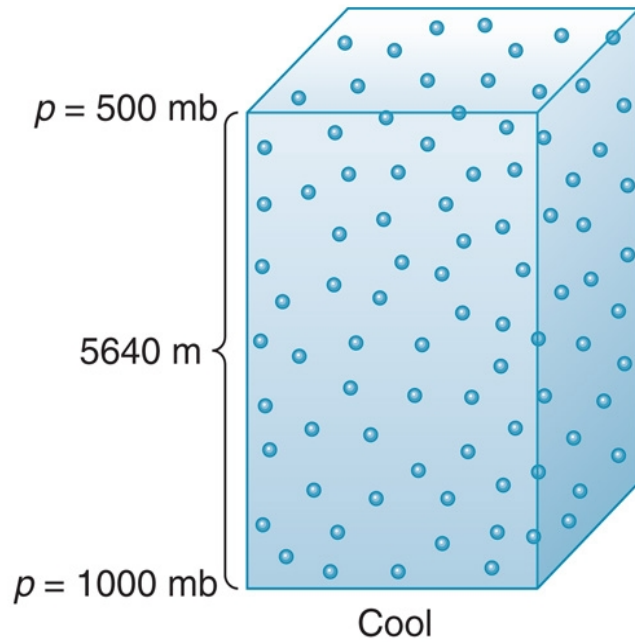
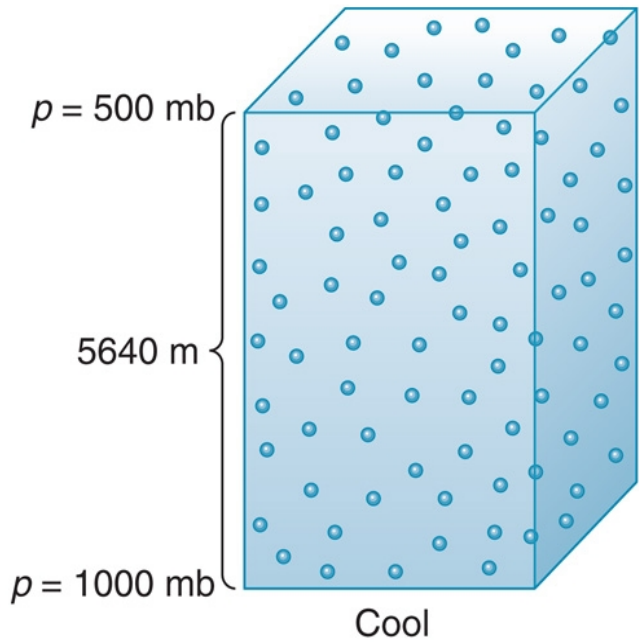
**These paragliders, initially at 900 hPa where temperature is 25°C, descend 100 m. What is the pressure at their new flight level?**

$$\rho_1, T_1 \text{ (known)} \quad \rightarrow \quad \rho_2, T_2$$

$$\rho_1 = \frac{p_1}{R T_1} =$$

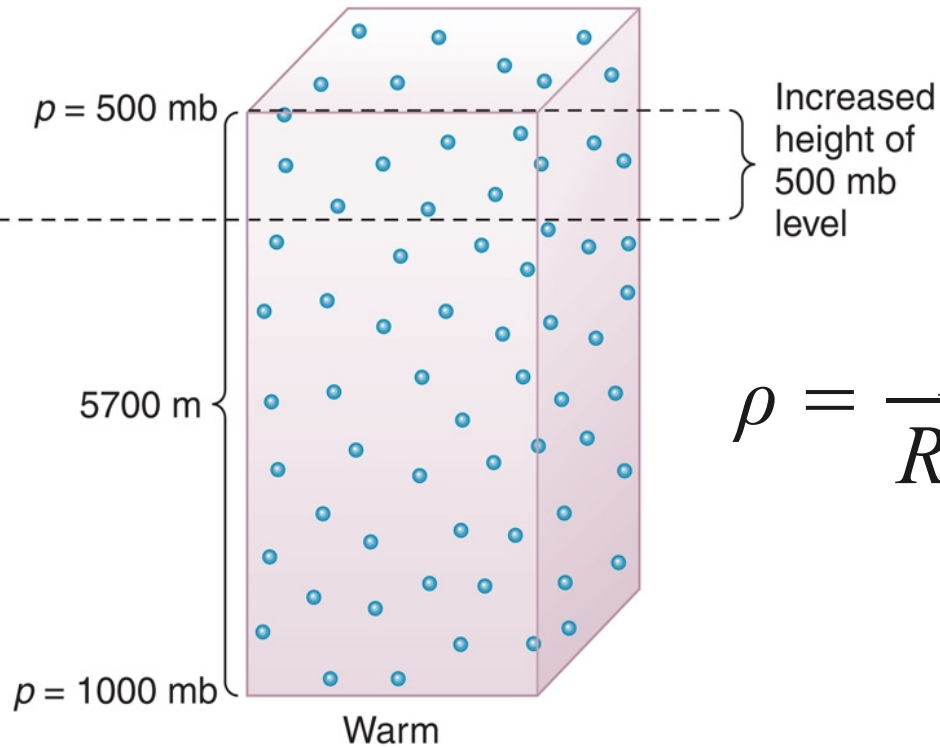
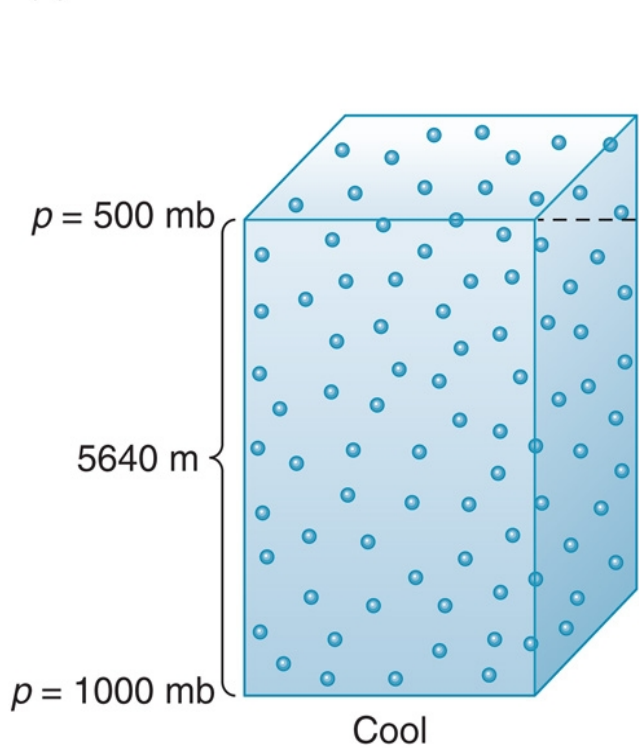


# Temperature controls rate of vertical decay of pressure



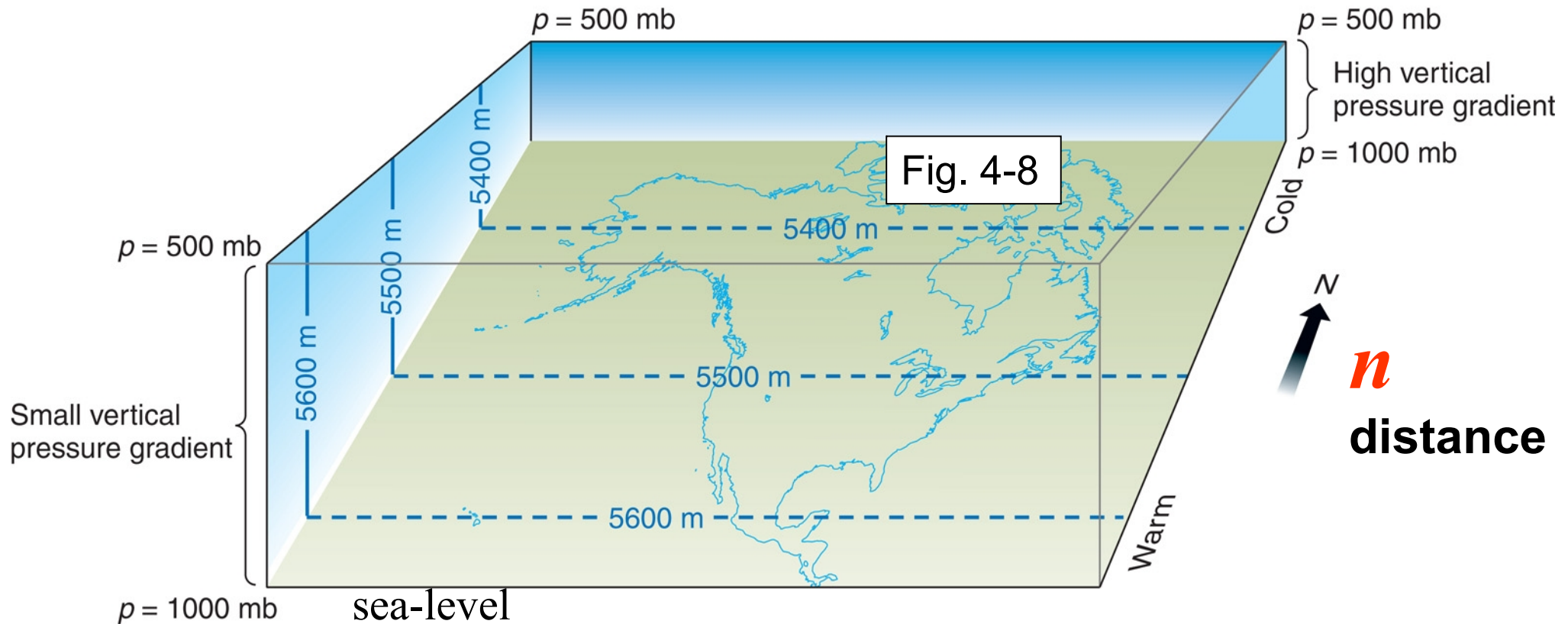
$$\frac{\Delta p}{\Delta z} = -\rho g$$

(a)



$$\rho = \frac{p}{R T} \propto \frac{1}{T}$$

Idealized sloping 500 hPa surface: height ( $h$ ) is lower in the colder, poleward air

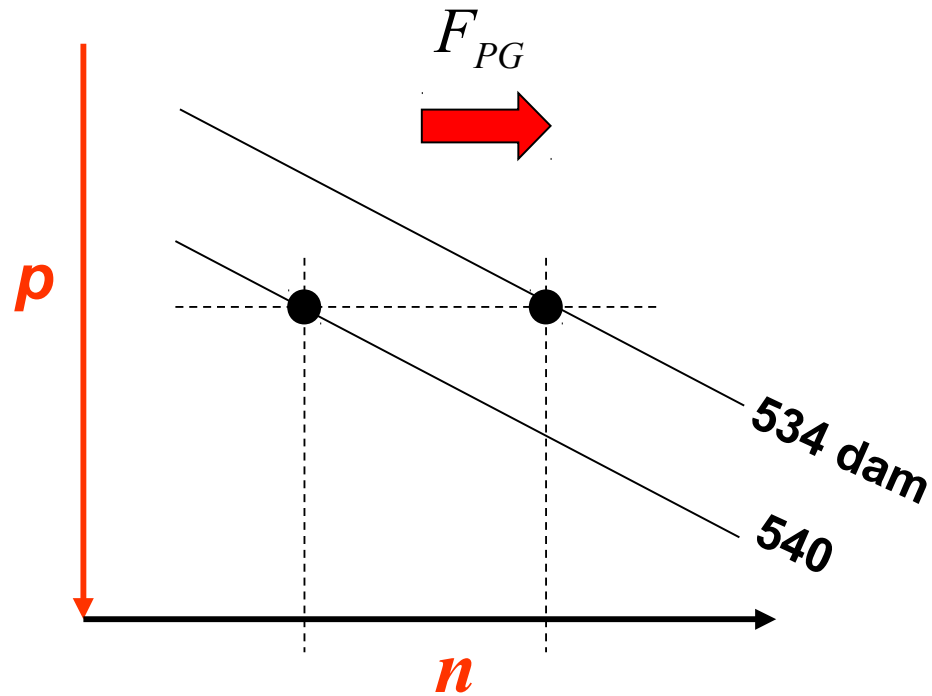


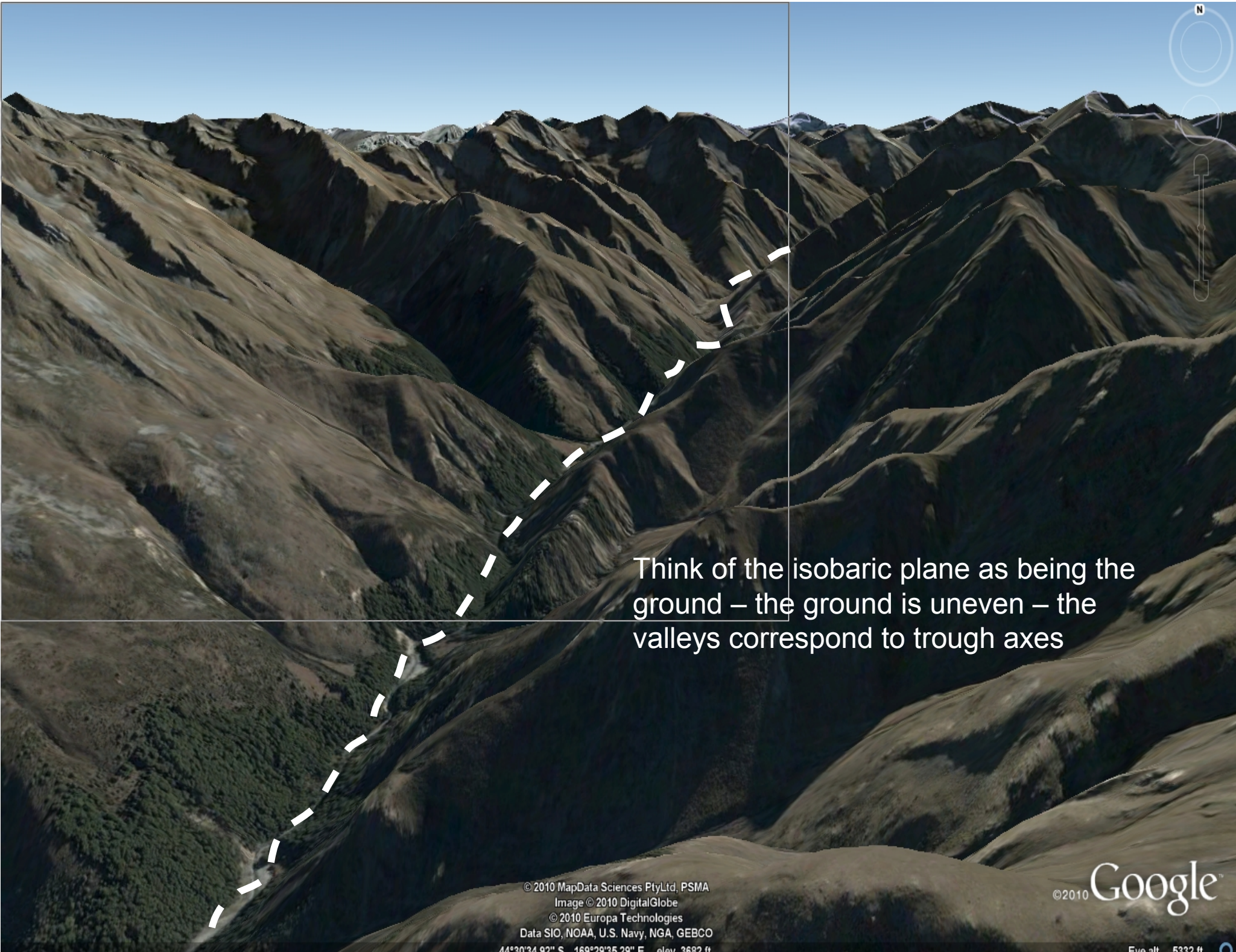
“Where a horizontal pressure gradient exists, there must also be a slope in the isobars\*\*, with heights decreasing toward colder air. It so happens that the horizontal pressure gradient force is proportional to the slope of the isobars.” (p112)

\*\* or isobaric planes, which are the constant pressure surfaces

Idealized sloping 500 hPa surface: height ( $h$ ) of the isobaric surface is lower in the colder, poleward air

**Note: direction of increase of  $p$ -axis**





Think of the isobaric plane as being the ground – the ground is uneven – the valleys correspond to trough axes

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Data SIO, NOAA, U.S. Navy, NGA, GEBCO

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44°30'34.92" S 169°29'35.29" E elev. 3682 ft

Eye alt 5332 ft

Aorangi  
(Mt. Cook)



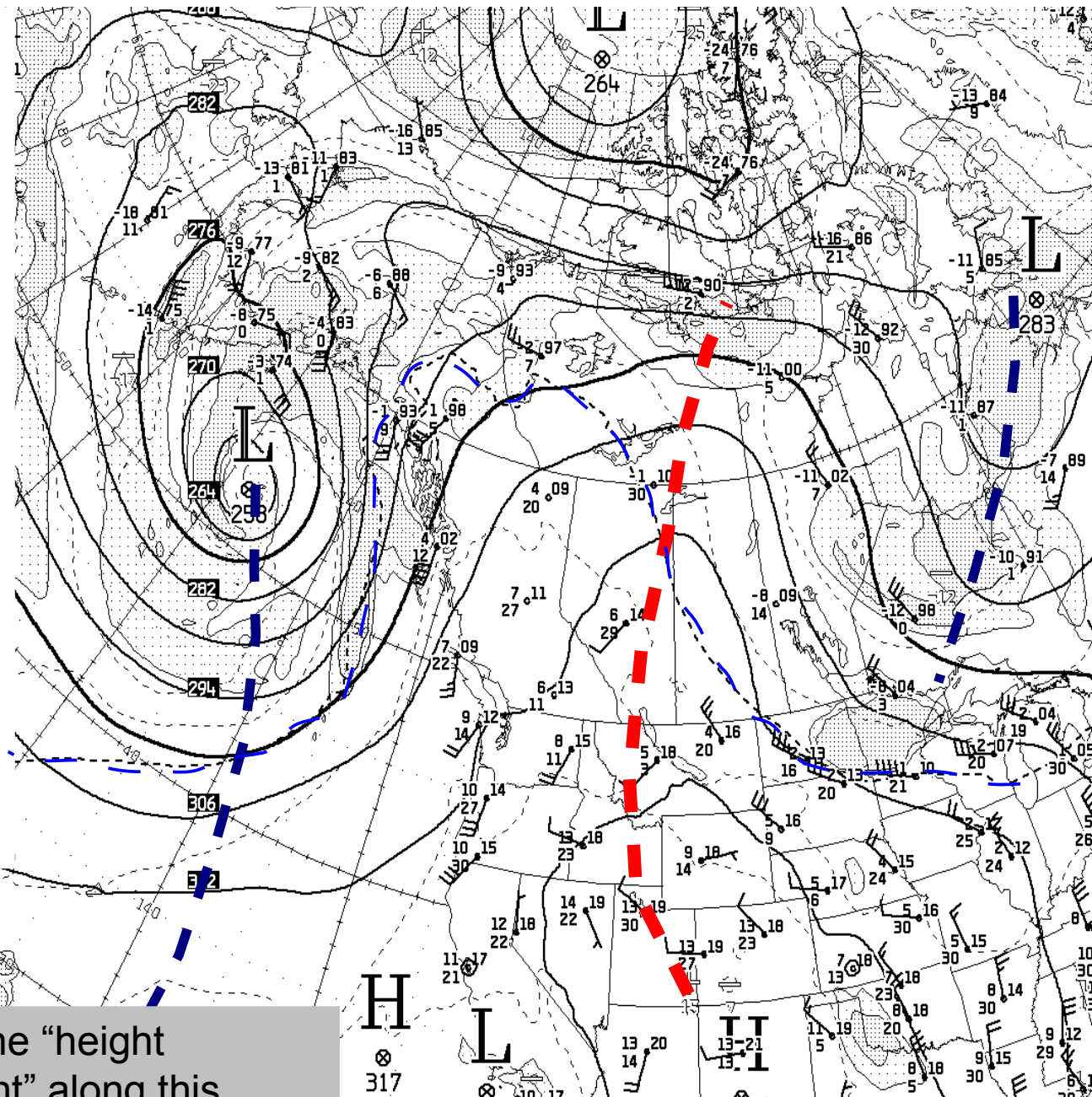
Queenstown, New Zealand



SIGNIFICANT WEATHER  
DISCUSSION ISSUED BY THE  
PRAIRIE AND ARCTIC STORM  
PREDICTION CENTRE OF  
ENVIRONMENT CANADA AT 7:00  
AM CDT FRIDAY OCTOBER  
1 2010.

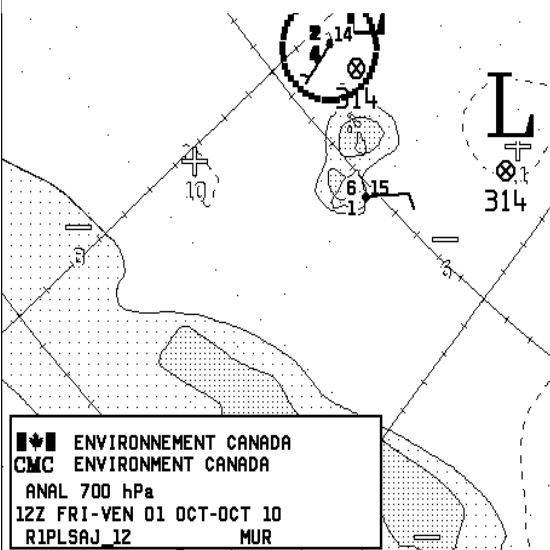
DISCUSSION...ALOFT, **BROAD  
UPPER RIDGE** OVER WESTERN  
CANADA AND **UPPER TROUGH**  
OVER HUDSON BAY...

SUNNY AND WARM FOR  
ALBERTA... NO SIGNIFICANT  
WEATHER IS EXPECTED OVER THE  
PRAIRIES OR ARCTIC OVER  
THE NEXT COUPLE OF DAYS



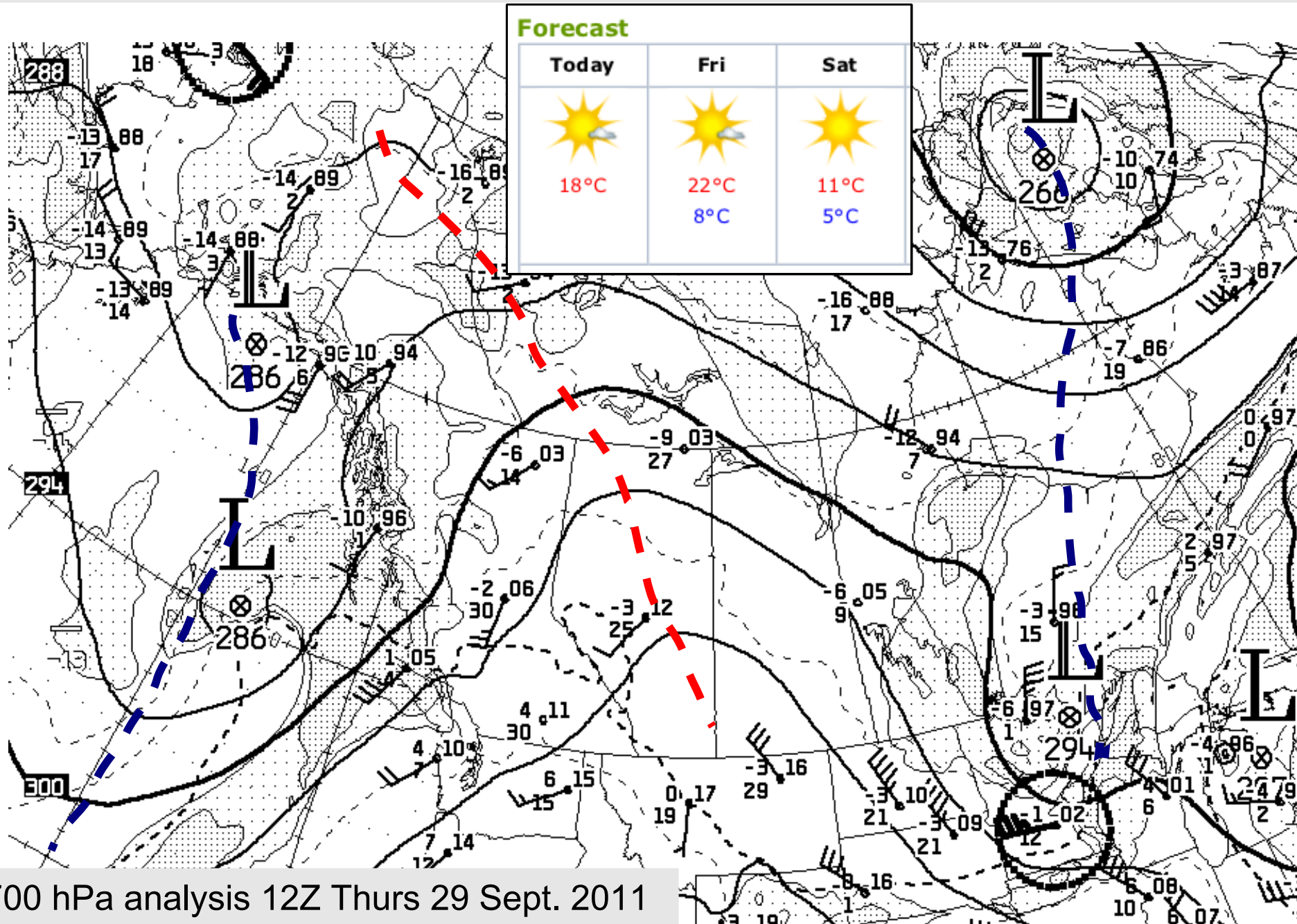
Note the “height  
gradient” along this  
**trough axis line** as we  
move towards the centre  
of the upper low

A **trough axis line** is analogous to a  
topographic valley – it is a valley on  
the isobaric surface (i.e. surface of  
constant pressure)



ENVIRONNEMENT CANADA  
CMC ENVIRONMENT CANADA  
ANAL 700 hPa  
12Z FRI-VEN 01 OCT-OCT 10  
RIPLSAJ 12 MUR

PRAIRIE AND ARCTIC STORM PREDICTION CENTRE 7:00 AM CDT THURS SEPT 29 2011...  
 OVERVIEW... UPPER LOW OVER WESTERN BAFFIN ISLAND WITH TROF SSWWD THRU  
 MANITOBA. WEAK RIDGE OVER BC LEAVING PRAIRIE IN WNWLY FLOW... NO SIGNIFICANT  
 WEATHER OVER EASTERN AND WESTERN PRAIRIES



MSC 700 hPa analysis 12Z Thurs 29 Sept. 2011

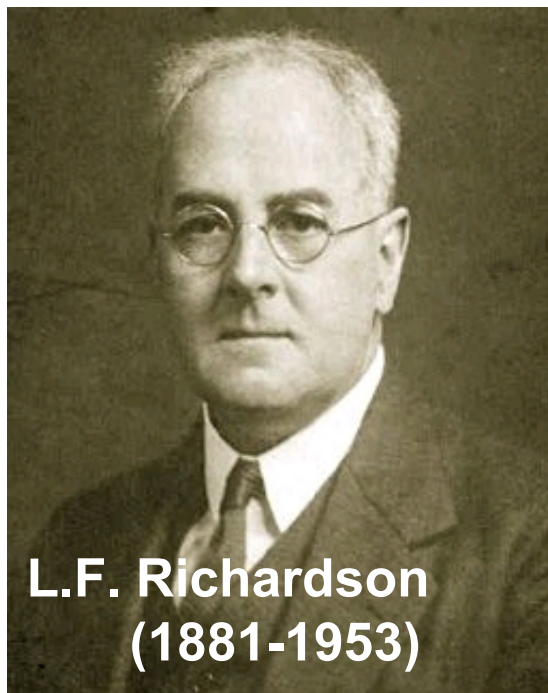
## A vast and continuous range of scales of motion (p246)

- Global scale  
Rossby waves...
- Synoptic scale (persist on timescale days-weeks)  
Highs & Lows, Monsoon, Foehn wind...
- Mesoscale (timescale hours)  
sea breeze, valley breeze...
- Microscale (timescale seconds-minutes)  
dust devils, thermals...
- and we don't give specific names to "turbulent eddies" whose scale spans (roughly) 100 m – 0.001 m (minutes to milliseconds)

• largest scales of motion are "quasi two-dimensional," meaning that ( $W \ll U, V$ ), due to thinness of troposphere (p5)

• smallest scales are three-dimensional and turbulent

## A vast and continuous range of scales of motion (p246)



**“Big whorls have little whorls,  
Which feed on their velocity;  
And little whorls have lesser whorls,  
And so on to viscosity.”**

- L.F. Richardson, 1922  
(parody of poem\*\* by Johnathon Swift, 1732)

“Great fleas have little fleas  
upon their backs to bite 'em,  
And little fleas have lesser  
fleas, and so *ad infinitum*.”

- ambulance driver, WW1 France
- in off-duty time, embarked on test of his mathematical weather forecasting method. Had with him in France observations for 7 a.m., 20 May 1910
- by 1916, had written *Weather Prediction by Arithmetic Finite Differences...*

This poem hints at the interaction and mutual interdependence of distinct scales of motion. Our focus for now is the synoptic scale horizontal wind