

**A. Dimensional Analysis**

Let  $U = U(x, z)$  represent the field of time-averaged wind speed about an infinitely-long, thin, porous windbreak fence that is oriented along the  $y$ -axis and thus perpendicular to the  $x$ -axis; let the angle of incidence of the mean wind relative to the fence be  $\beta$ . By symmetry, wind statistics are invariant along the axis ( $y$ ) parallel to the fence, and so vary only with distance ( $x$ ) normal to the fence, and with height ( $z$ ). The windbreak has height  $h$  and porosity  $\phi$ , while the state of the surface layer flow upwind of the windbreak is characterized by the friction velocity  $u_{*0}$ , the Obukhov length  $L$ , the depth of the boundary layer  $\delta$ , and the surface roughness length  $z_0$ . On the principle of being cautious – unduly cautious – let’s throw in properties of the fluid itself, namely mean density  $\rho$  and mean Kelvin temperature  $T$ .

Perform a dimensional analysis to determine the (dimensionless) factors upon which normalized mean windspeed  $U/u_{*0}$  might depend. Please report your results in an orderly way, and include a classification of the variables: e.g.  $x, z$  are coordinates, while  $h$  is a characteristic of the windbreak disturbing the flow. (Notes:  $\beta$  and  $\phi$  are dimensionless properties. You probably do not need to use the method of indices, i.e. you may be able to find the needed ratios by inspection).

**B. Computation of micrometeorological statistics**

The accompanying data file ‘utah.dat’ (6.75 MB) contains a time series of wind and temperature registered at 20 Hz and covering one hour, from two sonic anemometers (1,2) at heights  $z_1 = 3$  m and  $z_2 = 25.69$  m standing on an isolated tower on a salt flat in Utah (24 May, 2005; the data span local midday). The data are arranged in columns in the order  $u_1, v_1, w_1, T_1, u_2, v_2, w_2, T_2$ , where  $u$  is the northerly component,  $v$  the easterly component and  $w$  is the vertical velocity. The number of entries ( $N$ ) in each column should be  $20 \times 3600$  (but may differ slightly, so either  $N$  should be computed from the number of lines of data read, or set slightly smaller than 72,000).

Write a program to read the data file, compute, and write to a file the following statistics for each of the two levels:

- mean velocity components  $U, V, W$  and mean wind direction  $\beta = \arctan(V/U)$
- Reynolds stress tensor

$$\mathbf{R} \equiv R_{ij} \equiv \overline{u'_i u'_j} = \begin{pmatrix} \sigma_u^2 & \overline{u'v'} & \overline{u'w'} \\ \overline{u'v'} & \sigma_v^2 & \overline{v'w'} \\ \overline{u'w'} & \overline{v'w'} & \sigma_w^2 \end{pmatrix}$$

- the friction velocity

$$u_*^4 = (\overline{u'w'})^2 + (\overline{v'w'})^2$$

- the turbulent temperature scale  $T_* = -\overline{w'T'}/u_*$
- the Obukhov length<sup>1</sup>

$$L = -\frac{u_*^3 T_0}{k_v g \overline{w'T'}}$$

where  $k_v = 0.4$  is the von Karman constant and  $T_0$  [K] is bulk air temperature.

- heat flux density  $Q_H = \rho c_p \overline{w'T'}$  (to compute the density, assume the local pressure was  $p = 820$  mb).

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<sup>1</sup> $L$  is negative in unstable stratification, and infinite in magnitude in a neutral atmosphere where  $\overline{w'T'} = 0$  by definition. It is sometimes called the ‘substrate of dynamic turbulence’, because in the region  $z/|L| \ll 1$  the influence of buoyancy on the turbulence is negligible relative to that of wind shear. Conversely, at  $z/|L| \gg 1$  buoyancy is the main generator of turbulent fluctuations.