EAS270, "The Atmosphere" 1^{st} Mid-term Exam 5 Oct. 2015

<u>Professor</u>: J.D. Wilson <u>Time available</u>: 50 mins <u>Value</u>: 25%

No formula sheets; no use of tablet computers etc. or cell phones. Formulae and data are provided at the back. Please record your multichoice answers on the scantron sheet. Respond to calculation questions on the pages provided: add your name, tear off and submit. (You may keep other pages of this exam.)

A. Multi-choice $(32 \ge 1/2 \rightarrow 16 \%)$

- 1. Suppose you are at a height in Earth's atmosphere where pressure P = 500 hPa, and let $m \, [\text{kg m}^{-2}]$ designate the total atmospheric mass per unit surface area lying above this level. Which is the best estimate for m?
 - (a) 1
 - (b) 5
 - (c) 1000
 - (d) 5000
 - (e) 50,000

2. Which statement about the troposphere is **false**?

- (a) its depth is of order 100 km
- (b) it is considered to be well mixed on a time scale of the order of days
- (c) it is the layer whose variability manifests as (or controls) "weather"
- (d) its lowest 1 km or so constitutes the atmospheric "boundary layer"
- (e) on average, its temperature decreases with increasing elevation
- 3. Which combination lists the most abundant gas in earth's homosphere, and its proportion?
 - (a) O_2 , 92%
 - (b) O₂, 78%
 - (c) Ar, 78%
 - (d) N_2 , 99%
 - (e) N_2 , 78%

- 4. The Martian atmosphere is composed mostly of CO₂. Neglecting all other gases, and taking the surface pressure on Mars to be 7 hPa, what is the surface density ρ if surface temperature is $T = -53^{\circ}$ C? (The specific gas constant for CO₂ is $R = 189 \text{ J kg}^{-1} \text{ K}^{-1}$.)
 - (a) $0.00017 \text{ kg m}^{-3}$
 - (b) 0.017 kg m^{-3}
 - (c) $-0.0007 \text{ kg m}^{-3}$
 - (d) 0.1 kg m^{-3}
 - (e) 1 kg m^{-3}
- 5. Isolines of which "secondary field" are plotted on the CMC isobaric charts for the 500 hPa level?
 - (a) MSLP
 - (b) height of the 500 hPa surface
 - (c) isohumes (isolines of relative humidity)
 - (d) 1000-500 hPa thickness (DZ)
 - (e) temperature-dewpoint spread
- 6. Which of the statements below in relation to the atmospheric pool is **false**?
 - (a) plant respiration is sink for O_2 while animal respiration is a source
 - (b) combustion of organic material (CH₂O + O₂ \rightarrow CO₂ + H₂O) is a sink for O₂ and a source for CO₂
 - (c) anaerobic decomposition is a source for CH_4
 - (d) volcanic eruptions are a source for CO_2
 - (e) photosynthesis (CO₂ + H₂O \rightarrow CH₂O + O₂) is a source for O₂ and a sink for CO₂
- 7. If the temperature and virtual temperature of an air sample are respectively T = 298 K and $T_v = 300$ K, what is the mixing ratio r of the sample in the [kg/kg] unit? [Note: $T_v = T (1 + 0.61 r)$, with temperatures in Kelvin and r in kg/kg].
 - (a) 0.011
 - (b) 0.11
 - (c) 1.1
 - (d) 11

- 8. Which statement in regard to atmospheric aerosols is **false**?
 - (a) gravitational settling rapidly removes aerosols of radius $R > 10 \,\mu {\rm m}$
 - (b) precipitation scavenging is an important mechanism for cleaning the air of fine aerosols (radius $R < 10 \,\mu\text{m}$)
 - (c) aerosol "number density" (measured in the unit m^{-3} , i.e. count per unit volume) is larger in marine air than in continental air
 - (d) secondary aerosols are formed when precursor gases react in the atmosphere
 - (e) aerosols interact with radiation, and serve as surfaces on which water vapour may condense
- 9. Which statement is **false**?
 - (a) "heat energy" is synonymous with (has the same meaning as) the "internal energy" of a system
 - (b) some types of internal energy do not participate (i.e. do not undergo transformation) in natural atmospheric processes
 - (c) Einstein's mass-energy equivalence law $E = m c^2$ is irrelevant for the budgeting of heat energy in the atmosphere
 - (d) temperature is a measure of (i.e. proportional to) the average kinetic energy of air molecules
 - (e) added (or subtracted) heat energy that produces no change in a system's temperature is called "latent heat," and is associated with the breakage (or formation) of inter-molecular bonds that accomplishes a phase change in the system's state
- 10. A parcel of dry air at the surface (z = 0 m) has a temperature of 20°C. It is lifted adiabatically to z = 700 m then sinks adiabatically to z = 500 m. What is its final temperature?
 - (a) 29°C
 - (b) 27°C
 - (c) 25°C
 - (d) 20°C
 - (e) 15°C

11. Suppose 0.5 kg of dry air is contained in a rigid volume of 2 cubic metres. Based on the 1^{st} law of thermodynamics in the form

$$\Delta q \left[J \, \mathrm{kg}^{-1} \right] = c_v \Delta T + P \Delta \alpha \tag{1}$$

where $\alpha \equiv 1/\rho$ is the specific volume, which value best approximates the change in temperature (final minus initial) if 10⁴ J of energy are added to this system? (Assume $c_v = 718 \,\mathrm{J\,kg^{-1}\,K^{-1}}$. The "system" is the 0.5 kg air sample.)

- (a) 0 K
- (b) -14 K
- (c) +14 K
- (d) +28 K
- (e) +56 K
- 12. Defining the volumetric sensible heat content of a parcel of air as $h = \rho c_p T [\mathrm{J m}^{-3}]$ and taking the ρc_p product as $10^3 [\mathrm{J m}^{-3} \mathrm{K}^{-1}]$, what is the value of the convective heat flux density $Q_x [\mathrm{J s}^{-1} \mathrm{m}^{-2}]$ if the *x*-component of the wind is $u = 5 \mathrm{m s}^{-1}$ and the temperature of the parcel is 300 K? (Shortcut: consider units).
 - (a) $1.5 \times 10^6 \,\mathrm{W \, m^{-2}}$
 - (b) 3×10^5 K
 - (c) $120 \,\mathrm{W}\,\mathrm{m}^{-3}$
 - (d) $120 \,\mathrm{W}\,\mathrm{m}^{-2}\,\mathrm{s}^{-1}$
 - (e) $1500 \,\mathrm{J}\,\mathrm{m}^{-3}$
- 13. Taking the conductivity of glass as $k = 1 \,[\mathrm{W \, m^{-1} \, K^{-1}}]$, what is the rate of conductive heat transfer across a window pane of area $1 \,\mathrm{m^2}$ and thickness $\Delta x = 2.5 \,\mathrm{mm}$ when the temperature difference across the pane is 4K?
 - (a) 1600 J
 - (b) 1600 W
 - (c) $160 \,\mathrm{W \, s^{-1}}$
 - (d) 100 W
 - (e) 10 W

- 14. Suppose a parcel of air at the surface had state $(P_1, T_1) = (930 \text{ hPa}, 285.15 \text{K})$. What is the parcel's temperature after it has been lifted adiabatically to the 850 hPa level? (Hint: Poisson's equation).
 - (a) 11.7°C
 - (b) $12.3^{\circ}C$
 - (c) 278 K
 - (d) 293 K
- 15. A commercial jet is flying at an altitude where the air pressure is 20 kPa and the temperature is 213.15 K (or -60° C). If exterior air is brought inside the aircraft and pressurized (adiabatically) to 80 kPa, what will be its temperature? (Again, Poisson's equation).
 - (a) 143.4° K
 - (b) 317 K (or 43.7°C)
 - (c) $-89.2^{\circ}C$
 - (d) $-129.8^{\circ}C$
- 16. The daily temperature cycle is sometimes idealised as a "wave", with maximum surface temperature occurring at (say) time $t = t_{0,\text{max}}$ and with the surface temperature swinging through a daily range ΔT_0 (warmest temperature minus coldest temperature). Which statement regarding soil heat transfer and the wave in temperature at some depth d is **false**?
 - (a) the daily temperature range ΔT_d at depth d obeys $\Delta T_d > \Delta T_0$
 - (b) the dominant mechanism for soil heat transfer is usually conduction
 - (c) the daily temperature maximum at depth d occurs later than $t_{0,\text{max}}$
- 17. Which is the closest estimate for the vertical gradient in pressure $[Pa m^{-1}]$ at sea level?
 - (a) 100
 - (b) 10
 - (c) 1
 - (d) 0.1
 - (e) 0.01

- 18. For moist air, the ideal gas law reads $P = \rho R_d T_v$ where R_d is the gas constant for dry air and T_v is the virtual temperature. Suppose water vapour is added to a sample ("A") of previously dry air whose state was (P, T), and then the resulting volume (sample "B") is adjusted back to the original pressure and temperature. Which statement is correct? "Relative to sample A, sample B has ...
 - (a) higher virtual temperature but lower density ρ "
 - (b) higher virtual temperature and higher density ρ "
 - (c) lower virtual temperature and lower density ρ "
 - (d) lower virtual temperature and higher density ρ "
- 19. Suppose a certain unsaturated layer of the troposphere were "well mixed". Which would best approximate its temperature stratification?
 - (a) temperature unchanging with increase or decrease in height
 - (b) temperature increasing by 1 degree Celcius per 100 m increase in height
 - (c) temperature decreasing by 1 degree Celcius per 100 m increase in height
 - (d) temperature increasing by 1 degree Celcius per 1000 m increase in height
 - (e) temperature decreasing by 1 degree Celcius per 1000 m increase in height
- 20. Consider a uniform, dry, bare soil illuminated by the summer sun, and suppose that at the upper and lower surfaces of a horizontal layer of the soil the values of the soil heat flux (" Q_z [W m⁻²]", positive for downward heat flow) were respectively

$$Q_z(z_1) = 25 \text{ W m}^{-2},$$

 $Q_z(z_2) = 20 \text{ W m}^{-2}.$

Adopting the 'symmetry assumption' that soil temperature T = T(z, t), which statement regarding the layer $z_1 \le z \le z_2$ is correct?

- (a) insufficient information is given to determine whether this soil layer is warming or cooling
- (b) Fourier's law of conduction implies that there must be horizontal heat flows Q_x, Q_y in the layer
- (c) this soil layer must be cooling
- (d) this soil layer must be warming

21. The instantaneous vertical flux of sensible heat may be expressed as the sum of convective and conductive contributions

$$Q = \rho c_p w T - k \frac{\Delta T}{\Delta z} ,$$

where w is the vertical wind speed, T is the temperature and $\Delta T/\Delta z$ its vertical gradient, k is the conductivity of air, and ρ , c_p have their usual meanings (air density and specific heat capacity). Which statement is **false**?

- (a) the term involving the $w \times T$ product gives the contribution to the flux due to bulk movement, ie. wind (the "convective" contribution)
- (b) the term involving the $\Delta T/\Delta z$ gives the contribution to the flux due to molecular motion (i.e. the "conductive" contribution)
- (c) the $w\times T$ term vastly exceeds (in magnitude) the $\Delta T/\Delta z$ term in the bulk of the troposphere
- (d) adjacent to solid surfaces (the ground, leaves, etc.) the $w \times T$ term is suppressed, and the $\Delta T/\Delta z$ term dominates (laminar boundary layer)
- (e) the quantity $\rho c_p T$ has the unit [J]
- 22. People hiking or climbing in the wilderness may carry a lightweight aluminized sheet or bag or foil, that can be used to conserve body heat when sleeping in cold conditions. What characteristic of the material makes it useful in this regard?
 - (a) its thermal conductivity, which is low
 - (b) its thermal conductivity, which is high
 - (c) its high infrared emissivity
 - (d) its high infrared absorbtivity
 - (e) its low infrared emissivity
- 23. Referring to Figure (1), select the correct pair of values for the temperature lapse rate in respectively the lower and the upper layers. (Note: a temperature *change* of 1°C is the same as a change of 1 K).

(a) -0.01 K m^{-1} , -0.005 K m^{-1} (b) -0.01 K m^{-1} , -0.002 K m^{-1} (c) -0.02 K m^{-1} , -0.002 K m^{-1} (d) -0.02 K m^{-1} , -0.005 K m^{-1}

- 24. If a certain body has longwave emissivity $\epsilon = 0.96$ and its temperature is $T = 18^{\circ}$ C, which answer below most closely states the wavelength λ_{\max} of the peak in its thermal emission spectrum and its full-spectrum rate of emission E of longwave radiation?
 - (a) $10 \,\mu \text{m}, \, 6 \times 10^{-3} \,\text{W} \,\text{m}^{-2}$
 - (b) $100 \,\mu \text{m}, \, 390 \,\text{W} \,\text{m}^{-2}$
 - (c) $10 \,\mu \text{m}$, $390 \,\text{W} \,\text{m}^{-2}$
 - (d) $1 \,\mu \text{m}, 410 \,\text{W} \,\text{m}^{-2}$
 - (e) $0.1 \,\mu \text{m}, 410 \,\text{W} \,\text{m}^{-2}$
- 25. Suppose a pool (or reservoir) for "X" contained $M = 10^8$ [kg] of this species, and that there was a balance between the fluxes $Q_{\rm in}$, $Q_{\rm out}$ of X into and out of the pool, with $Q_{\rm in} = Q_{\rm out} = 10^{-4}$ [kg s⁻¹]. What is the residence time for X in this pool?
 - (a) 10^{-4} s
 - (b) 10^4 s
 - (c) 10^{-4} s $+10^{8}$ s
 - (d) 10^{12} s

For the remaining questions, please refer to Figures (2 - 3).

26. Referring to Figure 2, this analysis relates to what level of the atmosphere?

- (a) surface
- (b) 850 hPa
- (c) 700 hPa
- (d) 500 hPa
- (e) 250 hPa
- 27. Referring to Figure 2, the flow is visualized at (roughly) which height above sea level?
 - (a) 1.5 km
 - (b) 3 km
 - (c) 5.5 km
 - (d) 10 km

- 28. Referring to Figure 2, which is the correct description of the wind over Central Alberta (Stony Plain radiosonde)?
 - (a) calm
 - (b) SW, about $2 \,\mathrm{m \, s^{-1}}$
 - (c) NE, about $2 \,\mathrm{m \, s^{-1}}$
 - (d) SW, about $10 \,\mathrm{m \, s^{-1}}$
 - (e) NE, about $10 \,\mathrm{m\,s^{-1}}$
- 29. Referring to Figure 2, the solid contours are isolines of which property?
 - (a) height of the isobaric surface
 - (b) temperature
 - (c) Greenwich Mean Time
 - (d) wind speed
 - (e) wind direction
- 30. Referring to Figure 2, what property of the air is represented by the stippling pattern?
 - (a) height of the isobaric surface
 - (b) temperature
 - (c) thickness of the 1000-500 hPa layer
 - (d) small temperature-dewpoint spread (high humidity)
- 31. Referring to Figure 2, which statement in regard to the low at the lower right of the map (south of Manitoba) is **false**?
 - (a) it is a closed upper low
 - (b) its central pressure is 315 hPa
 - (c) the wind blows anticlockwise around its centre
 - (d) it is liable to be a slow moving feature
- 32. Referring to the location marked "X" on Figure 3, which statement is **false**?
 - (a) the heavy dashed line just N of the spot is the 0°C isotherm
 - (b) the lighter dashed line just S of the spot is the $+5^{\circ}$ C isotherm
 - (c) it is liable to get warmer at ${\bf X}$ in the following few hours
 - (d) the solid lines are isolines of the height of the 850 hPa surface (i.e. height contours)
 - (e) at the centre of the low (NE of ${\bf X})$ the isobaric surface drapes down to a local minimum height of 115 dam ASL

Continue to Calculations on the next THREE pages (3 x 3 \rightarrow 9 %).

B. Computations $(3 \times 3 \rightarrow 9 \%)$

Show your working, as you may receive part marks even if your answer is wrong.

B1. Compute the amount of energy a freezer must remove in order for 1 kg of water at 20°C to be made into a block of ice at -15° C. The specific heat of water is $c_w = 4186 [J \text{ kg}^{-1} \text{ K}^{-1}]$; for ice $c_i = 2100 [J \text{ kg}^{-1} \text{ K}^{-1}]$; and the latent heat of freezing is $L_f = 3.34 \times 10^5 [J \text{ kg}^{-1}]$. Give your answer to three significant digits¹, and state its units.

¹e.g. 1.23 or 123 or 0.0123 or 1.23×10^{-2} .

B2. Suppose that the ground-level pressure observed in Fort Smith (204 m ASL) was 978 hPa and that the corresponding sea-level corrected value ("MSLP") entered on the surface analysis was 1002.7 hPa (which would be coded as 027). What value had been assumed for the average virtual temperature \overline{T}_v of the (fictitious) 0-204 m layer at the station? Give your answer in Kelvin with five significant digits.

B3. The total flux of sensible heat along the vertical axis z may be written

$$Q \left[W m^{-2} \right] = \rho c_p w T - k \frac{\Delta T}{\Delta z}$$

where the first term is the convective contribution (usually by far the dominant part), and the second term is the conductive contribution. Compute a representative value for the ratio of the magnitudes of the terms contributing to the heat flux (conductive term divided by convective term), for a layer near sea level $(\rho c_p \approx 10^3 \,\mathrm{J\,m^{-3}\,K^{-1}})$ in which the vertical wind $w = +0.05 \,\mathrm{[m\,s^{-1}]}$, the temperature $T \approx 300 \,\mathrm{K}$ and the temperature lapse rate $\Delta T/\Delta z$ is the dry adiabatic rate (take the molecular conductivity of air to be $k = 0.025 \,\mathrm{[W\,m^{-1}\,K^{-1}]}$).

Equations and Data.

- P = M g/A, the pressure (P, Pa) that results when mass M [kg] overlies area A [m²], where g = 9.81 [m s⁻²]
- one full barb on the wind vector means 5 m s⁻¹, a solid triangle 25 m s⁻¹.
- $\frac{\Delta P}{\Delta z} = -\rho g$. ΔP [Pascals], the change in pressure as one ascends a distance Δz [m]; ρ [kg m⁻³] the air density; g = 9.81 [m s⁻²] grav. acceleration.
- $P = \rho R_d T_v$. The ideal gas law. P [Pascals], total pressure; ρ , [kg m⁻³] the total density; T_v [Kelvin], the virtual temperature; and $R_d = 287$ [J kg⁻¹ K⁻¹], the specific gas constant for dry air.
- $T_v = T (1 + 0.61 r)$. Defines the virtual temperature [K] of an air sample whose temperature is T [K] and whose water vapour mixing ratio is r [kg/kg].
- $\Delta q = c_v \Delta T + P \Delta \alpha$. The first law of thermodynamics, linking changes in the state of a sample of air: $\Delta q \; [\mathrm{J \; kg^{-1}}]$ is energy added to the system (zero for an adiabatic process, by definition), c_v is the specific heat capacity of the material at constant volume, P is the pressure and $\alpha \equiv 1/\rho$ is the specific volume (ρ being air density). For an ideal gas $c_v = (5/2)R$, so that for dry air $c_v \approx 718 \; \mathrm{J \; kg^{-1} \; K^{-1}}$.

$$\frac{T}{T_1} = \left(\frac{P}{P_1}\right)^{R/c_p}$$

Poisson's law linking two states (P, T) and (P_1, T_1) of a sample of ideal gas, assuming the process connecting the two states is adiabatic $(R/c_p = 2/7 = 0.286)$.

• $\frac{\Delta T}{\Delta z} = -g/c_p$. The dry adiabatic lapse rate, where g is the gravitational acceleration and $c_p \approx 1000 \, [\mathrm{J \, kg^{-1} \, K^{-1}}]$ is the specific heat at constant pressure.

$$Q_x = -k \frac{\Delta T}{\Delta x}, \ Q_y = -k \frac{\Delta T}{\Delta y}, \ Q_z = -k \frac{\Delta T}{\Delta z}$$

Fourier's law of conduction, giving the components (Q_x, Q_y, Q_z) of the conductive heat flux density along directions (x, y, z) in response to temperature gradients $\Delta T/\Delta x$ (etc.) along the axes in a medium whose conductivity is $k [\text{W m}^{-1} \text{K}^{-1}]$. (The sign convention is that Q_x is positive for a flow of heat towards larger values of x, etc.) $\bullet \ E \ = \ \epsilon \ \sigma \ T^4$

Stefan-Boltzmann law for a greybody. $E \, [W m^{-2}]$, the emitted longwave energy flux density; ϵ , the emissivity of the surface (dimensionless); $\sigma = 5.67 \times 10^{-8} \, [W m^{-2} K^{-4}]$, the Stefan-Boltzmann constant; $T \, [K]$, the surface temperature.

•
$$\lambda_{\max} = \frac{2897}{T}$$

Wien's displacement law. λ_{max} [μ m], the wavelength at which the peak in the emission spectrum occurs; T [K], the temperature of the emitting surface.



Figure 1: Idealized profile of temperature in the lowest 1500 m of the atmosphere. The "elbow" is at $(z, T) = (500 \text{ m}, 15^{\circ} \text{C})$.



Figure 2: Environment Canada analysis (cropped) for 12 UTC 25 September 2015. Dashed lines are isotherms, with 5° C interval.



Figure 3: Environment Canada 850 h Pa analysis (cropped) for 00 UTC 13 September 2015. Height contours are at 6 dam interval.