

Professor: J.D. WilsonTime available: 50 minsValue: 25%No formula sheets; no use of tablet computers etc. or cell phones. **Formulae/data at back.****Multi-choice (25 x 1 → 25 %)**1. Referring to Figure (1), which statement is **false**?

- (a) A,B,C lie in the shortwave radiation band
- (b) D,E lie in the longwave radiation band
- (c) The atmosphere is almost completely transparent at C
- (d) Waveband C would be ideal for nocturnal viewing of earth from satellites **XX**
- (e) The high absorbtivity at $\lambda > 20 \mu\text{m}$ is due to greenhouse gases

2. Referring to Figure (2), select the correct pair of values for the temperature lapse rate ($\Delta T/\Delta z$) in respectively the lower and the upper layers. (Note: a temperature *change* of 1°C is the same as a change of 1 K).

- (a) -0.01 K m^{-1} , -0.005 K m^{-1}
- (b) -0.01 K m^{-1} , -0.002 K m^{-1} **✓✓** Read $\Delta T/\Delta z$ off graph.
- (c) -0.02 K m^{-1} , -0.002 K m^{-1}
- (d) -0.02 K m^{-1} , -0.005 K m^{-1}
- (e) -0.05 K m^{-1} , -0.005 K m^{-1}

3. Referring to Figure 3, which option gives correct units for the vertical axis (spectral emission rate from a black body) and for the area under the curve (emitted radiant energy flux density)?

- (a) W m^{-2} , W m^{-2}
- (b) $\text{W m}^{-2} \mu\text{m}^{-1}$, W
- (c) $\text{W m}^{-2} \mu\text{m}^{-1}$, W m^{-2} **✓✓**
- (d) $\text{W m}^{-2} \mu\text{m}^{-1}$, $\text{W} \mu\text{m}^{-1}$
- (e) $\text{W} \mu\text{m}^{-1}$, $\text{W} \mu\text{m}$

4. If a certain body has longwave emissivity $\epsilon = 0.96$ and its temperature is $T = 18^\circ\text{C}$, which option most closely states the wavelength λ_{max} of the peak in its thermal emission spectrum and its full-spectrum rate of emission E of longwave radiation?

- (a) $10 \mu\text{m}$, 390 W m^{-2} **✓✓**
- (b) $10 \mu\text{m}$, $6 \times 10^{-3} \text{ W m}^{-2}$
- (c) $100 \mu\text{m}$, 390 W m^{-2}
- (d) $1 \mu\text{m}$, 410 W m^{-2}
- (e) $0.1 \mu\text{m}$, 410 W m^{-2}

5. Which statement in regard to Figure (4) is **false**?
- (a) each of Q^* , Q_H , Q_E quantifies an energy flux density oriented along the *vertical* axis
 - (b) it is implicit (assumed) horizontal energy flows are irrelevant
 - (c) above the laminar sublayer on ground surfaces, the transport mechanism for sensible & latent heat (Q_H , Q_E) is convection
 - (d) Q_G (sometimes symbolized ΔQ_S) is the rate at which energy is stored/released below the reference plane
 - (e) times of sunrise & sunset coincide with sign changes in net radiation (Q^*) **XX**
6. Suppose on a sunny summer afternoon the net radiation over a flat field of bare soil were $Q^* = 500 \text{ W m}^{-2}$, and the sensible and latent heat fluxes were $Q_H = 180$, $Q_E = 300 \text{ W m}^{-2}$. What was the soil heat flux Q_G ?
- (a) 980 W m^{-2}
 - (b) 480 W m^{-2}
 - (c) 120 W m^{-2}
 - (d) 20 W m^{-2} **✓✓**
 - (e) -980 W m^{-2}
7. Compute absolute humidity ρ_v if vapour pressure $e = 1.1 \text{ kPa}$ and temperature $T = 23^\circ\text{C}$.
- (a) $8 \times 10^{-3} \text{ kg m}^{-3}$ **✓✓**
 - (b) $8 \times 10^{-6} \text{ kg m}^{-3}$
 - (c) 0.1 kg m^{-3}
 - (d) $1 \times 10^{-4} \text{ kg m}^{-3}$
 - (e) 8 g kg^{-1}
8. What is the RH of air with temperature $T = 6^\circ\text{C}$ and vapour pressure $e = 7 \text{ hPa}$?
- (a) 95%
 - (b) 75% **✓✓**
 - (c) 65%
 - (d) 55%
 - (e) 45%
9. Which property is **not** constant, for an air parcel undergoing unsaturated, adiabatic vertical motion?
- (a) mixing ratio r
 - (b) specific humidity q
 - (c) potential temperature θ
 - (d) vapour pressure e **XX**

10. Suppose planet A at distance r_A from its star (or sun) has solar constant S_A . What is the solar constant (“ S_B ”) for planet B, orbiting the same star at distance $r_B = 4r_A$?
- (a) $4S_A$
 - (b) $16S_A$
 - (c) $S_A/4$
 - (d) $S_A/16$ ✓✓
 - (e) $S_A/64$

11. A hypothetical “radiative equilibrium temperature” T_E can be calculated as the mean temperature of an isothermal earth (of radius r_E) that has no atmosphere, based on an energy balance of form

$$\frac{dT_E}{dt} \propto \pi r_E^2 (1 - r_s) S_0 - 4\pi r_E^2 \sigma T_E^4$$

I *II* *III*

where the term on the left is the rate of warming or cooling (change in T_E per unit change in time t), r_s is the albedo (shortwave reflectivity), S_0 the solar constant, σ the Stefan-Boltzmann constant, and \propto means “is proportional to”. Which term(s) is/are set to zero in order to compute the radiative equilibrium temperature?

- (a) I ✓✓
- (b) I, II
- (c) I, III
- (d) I, II, III
- (e) III

12. Suppose a pilot, flying at midday through the middle of a deep cloud layer, observes a brighter region towards the sun. Which best describes the colour of this sunlight?
- (a) reddish light
 - (b) bluish light
 - (c) milky white light ✓✓
 - (d) yellow-brown light

13. At the time of the southern hemisphere summer solstice (solar declination $\delta = -23.5^\circ$), what is the noon solar elevation at latitude $\phi = +23.5^\circ$ (which is in the northern hemisphere)? (See given equation)
- (a) 90°
 - (b) 66.5°
 - (c) 43° ✓✓
 - (d) 23.5°
 - (e) 0°

14. Based on Figure (5), at what time did the daily maximum in surface temperature occur?
(Note: Local Standard Time was UTC - 7).
- (a) 0/24 UTC
 - (b) 21 UTC ✓✓
 - (c) between 19 and 20 UTC
 - (d) 13 UTC
 - (e) 3 UTC
15. Assuming Figure (6) applies during a period of cloudless summer weather, which interpretive statement is **false**?
- (a) the layer identified as “free air” also classifies as being an inversion
 - (b) the “Residual Layer” is well-mixed (i.e. neutral) with respect to unsaturated adiabatic motion
 - (c) this diagram is characteristic of mid-afternoon conditions ✗✗
 - (d) the “free air” is unconditionally stable
 - (e) the sensible heat flux Q_H is negative in the surface inversion, and zero in the Residual Layer
16. Referring to Figure (7), over what interval of time was the atmospheric surface layer unstably stratified?
- (a) midnight to 07:00
 - (b) 17:30 to midnight
 - (c) midnight to 07:00 and 17:30 to midnight
 - (d) 07:00 to 17:30 ✓✓
 - (e) 05:30 to 20:00
17. Referring to Figure (8), what is the temperature T if the vapour pressure is $e = 4$ kPa?
- (a) -20°C
 - (b) 0°C
 - (c) 20°C
 - (d) 29°C
 - (e) T cannot be determined from the given information ✗✗

18. Referring to Figure (9), which statement is **true**?
- (a) the middle layer is neutral with respect to unsaturated adiabatic motion ✓✓
 - (b) until it rose above level z , an unsaturated parcel rising from the surface would be subject to a downward buoyancy force F_B
 - (c) in middle layer, potential temperature decreases with increasing height
 - (d) the uppermost layer is absolutely unstable
 - (e) the surface layer is an inversion
19. Using Figure (10), deduce an *approximate* value for the potential temperature of air with $(P, T) = (400 \text{ hPa}, -60^\circ\text{C})$, taking the reference pressure as 1000 hPa.
- (a) -22°C
 - (b) -22K
 - (c) -2°C
 - (d) $+4^\circ\text{C}$ ✓✓
 - (e) $+22^\circ\text{C}$
20. Again referring to Figure (10), suppose the surface pressure, temperature and dewpoint were respectively (1000hPa, 10°C , -20°C). Using Normand's Rule, estimate the pressure at the Lifting Condensation Level.
- (a) 510 hPa
 - (b) 630 hPa ✓✓
 - (c) 680 hPa
 - (d) 850 hPa
 - (e) 1000 hPa
21. If the Level of Free Convection is at height $z_{\text{LCL}} = 500 \text{ m}$ AGL (above ground level) and the surface temperature is $T = 23^\circ\text{C}$, what is the surface dewpoint T_d ?
- (a) -4°C
 - (b) 4°C
 - (c) 11.5°C
 - (d) 19°C ✓✓
 - (e) 27°C

22. What is signified by the heavy dashed line on Figure (11) that has been added by the instructor?
- (a) ridge in the 500 hPa height field
 - (b) trough in the 500 hPa height field
 - (c) thermal (thickness) ridge ✓✓
 - (d) thermal trough
 - (e) possibility of freezing rain
23. What is signified by the pattern of stippling on Figure (11)?
- (a) possibility of freezing rain
 - (b) thickness lies in the interval $534 \leq \Delta Z \leq 540$ dam ✓✓
 - (c) temperature-dewpoint spread $T_{\text{dd}} \leq 2$ K
 - (d) temperature below freezing
 - (e) probable path for the upper low to follow
24. Based on Figure (11), which statement regarding the short term (say, 1 hour) weather trend at the point denoted “X” (north of “SASK.”) is most plausible?
- (a) advective warming ✓✓
 - (b) advective cooling
 - (c) radiative cooling
 - (d) frost
 - (e) rain
25. Referring to Figure (12), which statement correctly distinguishes the expected 1-hour advective temperature trends at the points (A,B,C)?
- (a) A warming, B cooling, C cooling
 - (b) A cooling, B warming, C cooling
 - (c) A unchanging, B warming, C warming
 - (d) A unchanging, B cooling, C warming ✓✓
 - (e) A warming, B warming, C warming

Equations and Data.

- $E = \epsilon \sigma T^4$. Stefan-Boltzmann law. E [W m^{-2}], the emitted longwave energy flux density; ϵ , the emissivity of the surface (dimensionless); $\sigma = 5.67 \times 10^{-8}$ [$\text{W m}^{-2} \text{K}^{-4}$], the Stefan-Boltzmann constant; T [K], the surface temperature.
- $\lambda_{\max} = \frac{2897}{T}$. Wien's displacement law. λ_{\max} [μm], the wavelength at which the peak in the emission spectrum occurs; T [K], the temperature of the emitting surface.
- $\alpha = 90^\circ - |\phi - \delta|$. Solar elevation α at local solar noon time, at a location having latitude ϕ (negative in the S. hemisphere), at the time of year when solar declination is δ (δ is negative during northern hemisphere winter, and at the time of the solstices its *magnitude* is 23.5°).
- $Q^* = Q_H + Q_E + \Delta Q_S$. Surface energy balance on a reference plane at the base of the atmosphere. Q^* the net radiation, positive if directed towards the surface; Q_H, Q_E the sensible and latent heat fluxes, positive if directed from the surface towards the atmosphere; ΔQ_S (sometimes denoted Q_G) the storage term, positive if directed from the surface into ground/lake/ocean.
- $e = \rho_v R_v T$. The ideal gas law for water vapor. e [Pa], vapour pressure; ρ_v , [kg m^{-3}] the absolute humidity (ie. vapor density); T [Kelvin], the temperature; and $R_v = 462$ [$\text{J kg}^{-1} \text{K}^{-1}$], the specific gas constant for water vapor.
- $F_B = g \frac{T_p - T}{T} = g \frac{\theta_p - \theta}{\theta}$. The buoyancy force on a parcel whose temperature is T_p (and potential temperature is θ_p) at a level where the environmental temperature and potential temperature are T, θ . The denominator must be in Kelvin unit. F_B is positive for an upward force.
- $z_{\text{LCL}} = 125 (T_{\text{sfc}} - T_{\text{d,sfc}})$. Gives the height of the LCL in metres AGL, given the difference between surface temperature and surface dewpoint.

Table 1: Equilibrium vapour pressure $e_s(T)$ [hPa] versus temperature T [$^\circ\text{C}$]. Figure cited applies to equilibrium over a plane surface of water where $T \geq 0^\circ\text{C}$, or of ice where $T < 0^\circ\text{C}$.

T	$e_s(T)$	T	$e_s(T)$	T	$e_s(T)$	T	$e_s(T)$	T	$e_s(T)$	T	$e_s(T)$	T	$e_s(T)$
-10	2.60	-5	4.02	0	6.11	5	8.72	10	12.27	15	17.04	20	23.37
-9	2.84	-4	4.37	1	6.57	6	9.35	11	13.12	16	18.17	21	24.86
-8	3.10	-3	4.76	2	7.05	7	10.01	12	14.02	17	19.37	22	26.43
-7	3.38	-2	5.17	3	7.58	8	10.72	13	14.97	18	20.63	23	28.09
-6	3.69	-1	5.62	4	8.13	9	11.47	14	15.98	19	21.96	24	29.83
				25	31.67	26	33.61	27	35.65	28	37.80	29	40.06

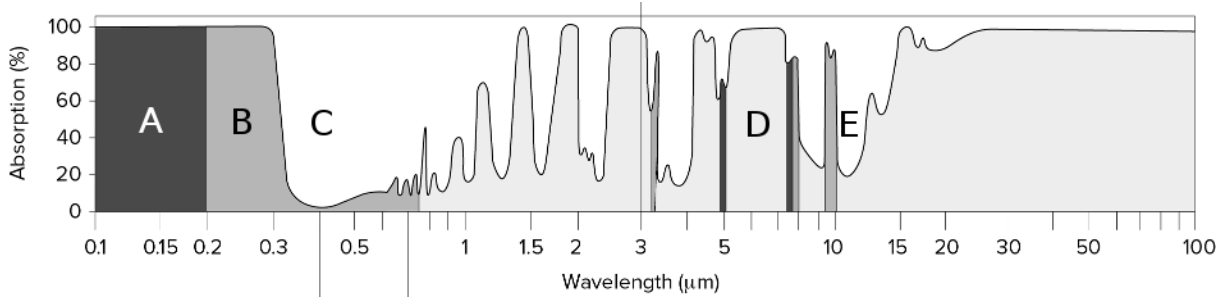


Figure 1: Radiative absorptivity of the earth’s atmosphere, versus wavelength (“ λ ”): if, at a given wavelength, the absorptivity is 100%, then light of that wavelength is absorbed completely on a vertical path through the (whole) atmosphere. Labels (A,B,...E) each denote a characteristic region of the absorption spectrum.

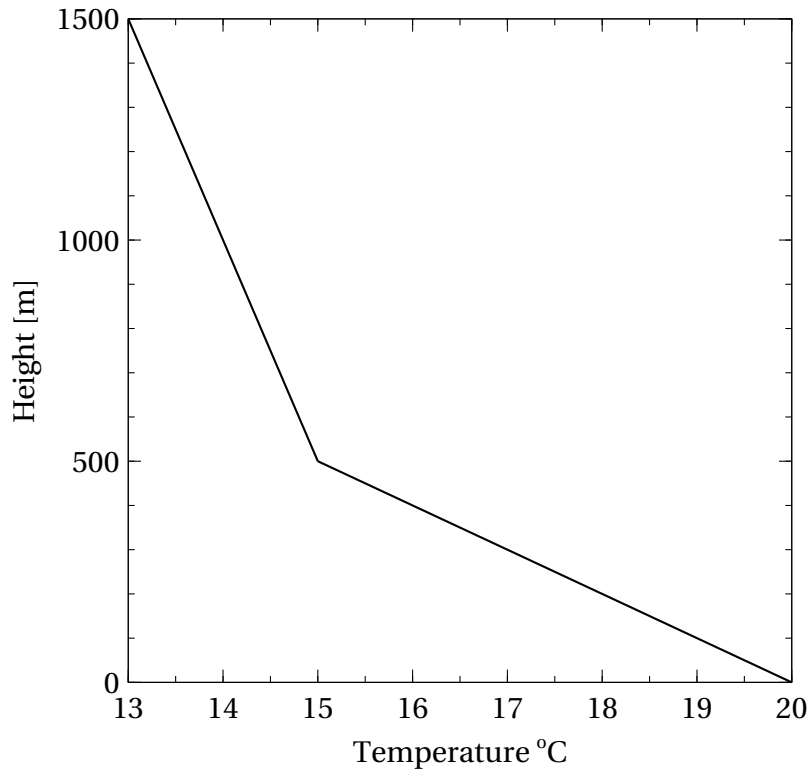


Figure 2: Idealized profile of temperature in the lowest 1500 m of the atmosphere. The “elbow” is at $(z, T) = (500 \text{ m}, 15^\circ\text{C})$. (Note: a temperature *change* of 1°C is the same as a change of 1 K.)

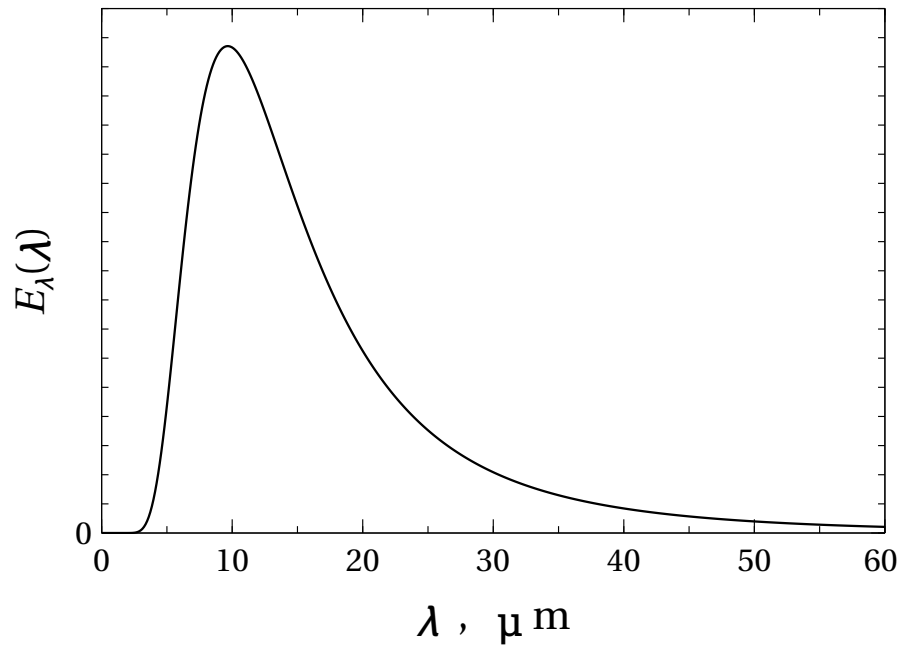


Figure 3: Planck curve for the spectral emission rate from a blackbody with temperature 300 K.

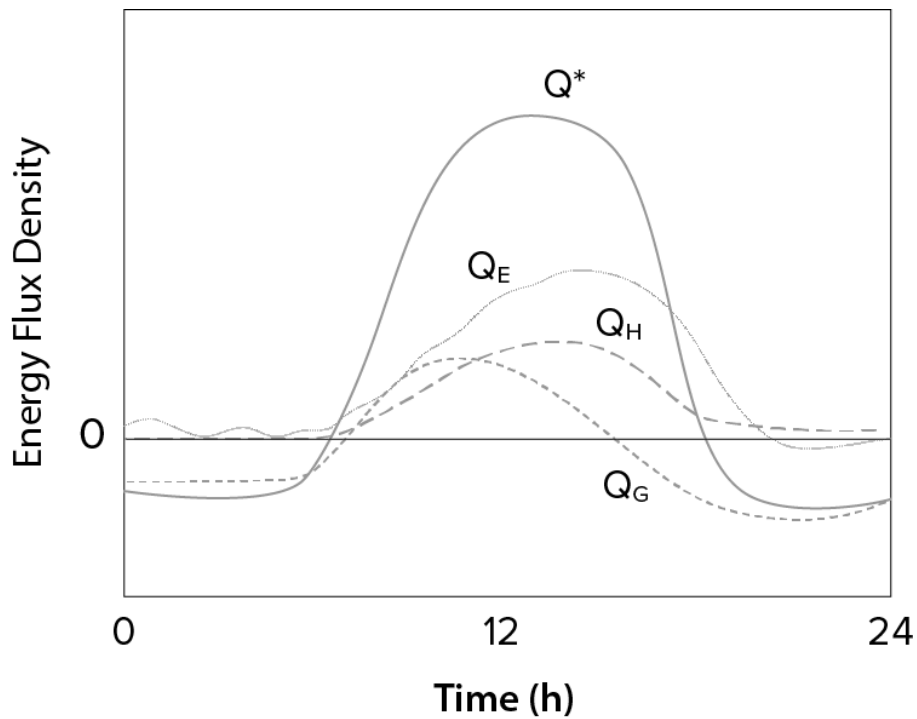


Figure 4: Idealized daily cycle in the components of the surface energy balance “for a moist, vegetated surface on a clear day in summer” (Figure 6.19 from Ross’s *Weather & Climate*). Symbols are Q^* the net radiation ($= K^* + L^*$, sum of net shortwave plus net longwave radiation), positive for downward flow towards the surface; Q_H, Q_E the sensible and latent heat fluxes, positive for upward flow away from the surface; and Q_G the energy flux into storage, sometimes labelled ΔQ_s .

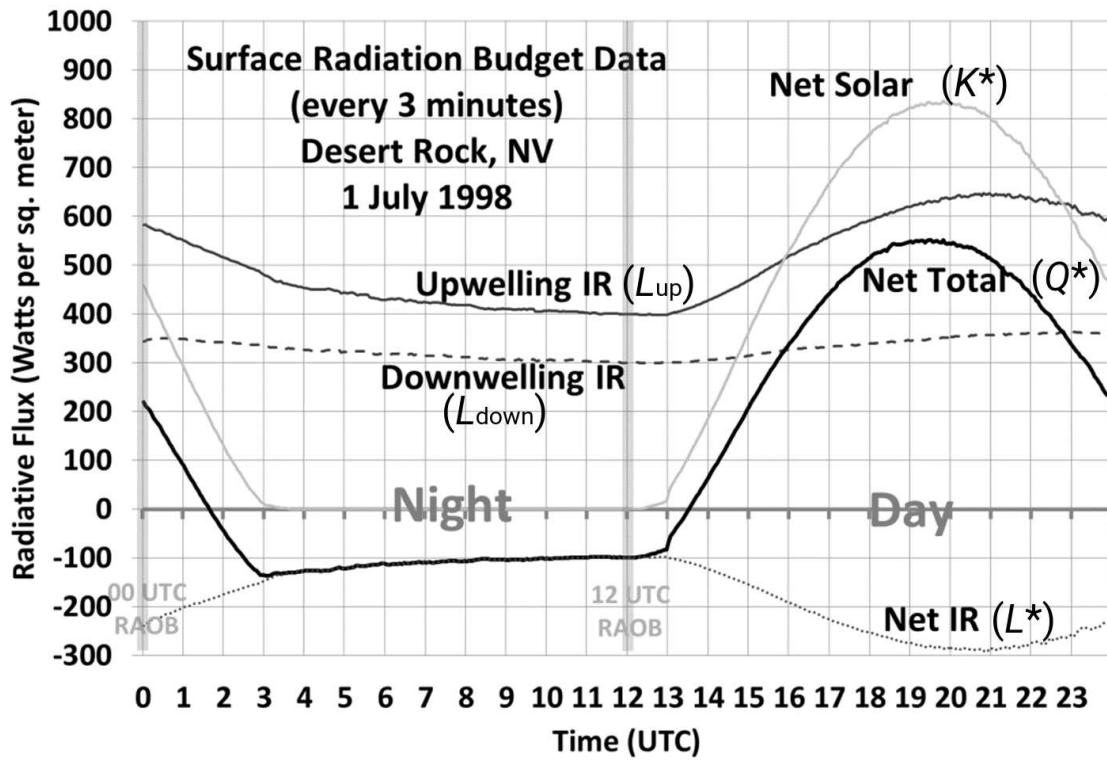


Figure 5: Variation with time of the components of the near-surface radiation budget, measured in Nevada.

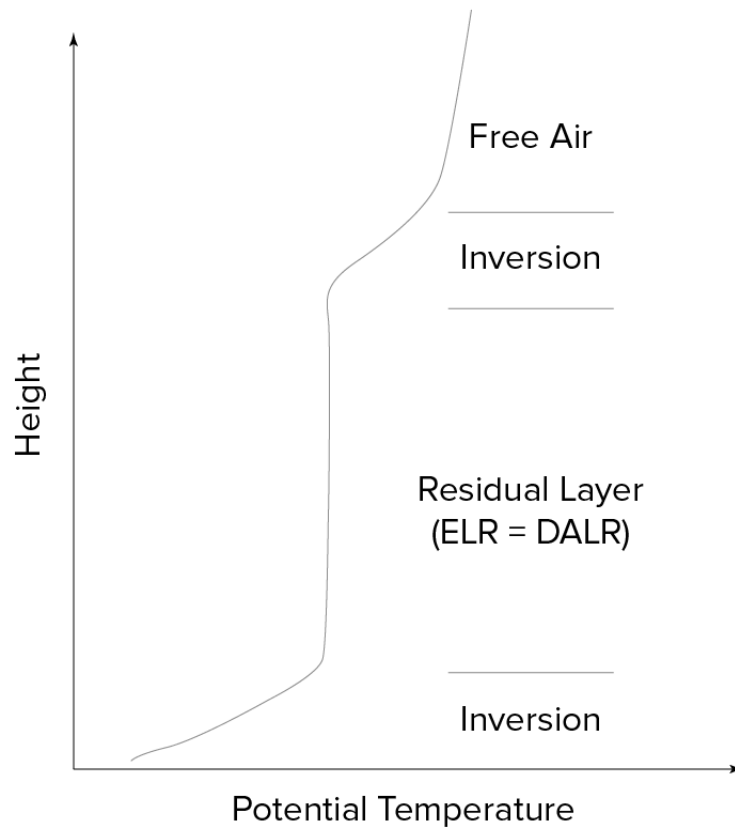


Figure 6: Idealised profile of potential temperature $\theta(z)$.

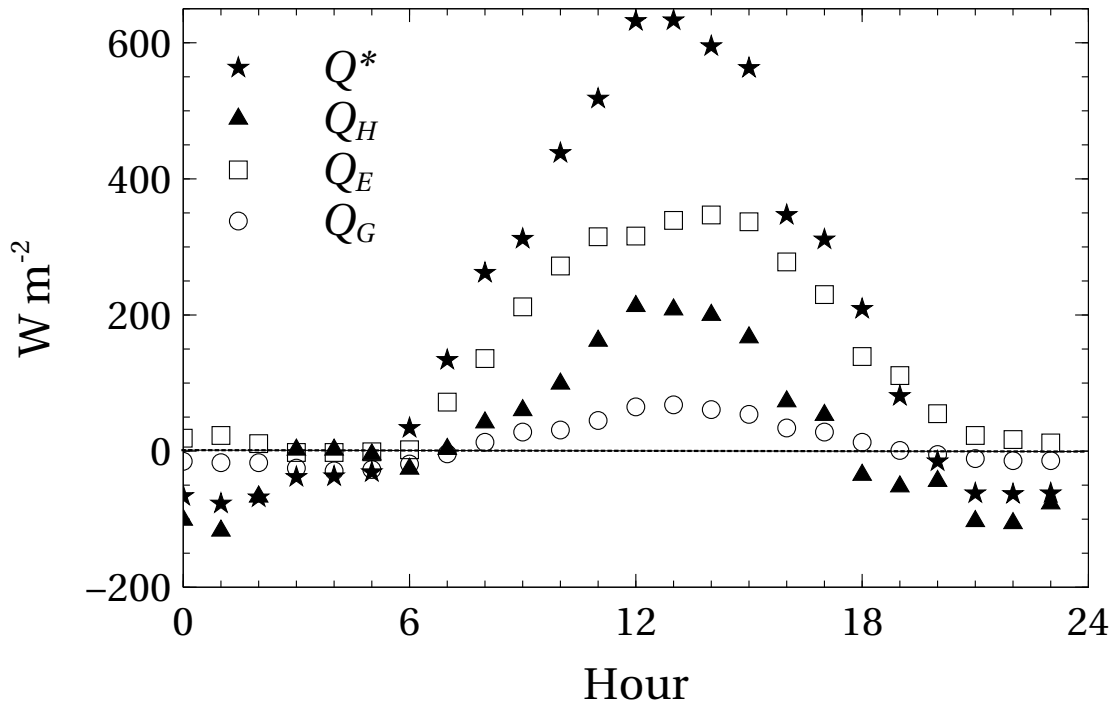


Figure 7: Variation with time of the components of the surface energy budget over grassland in Alberta (1 July 2003; courtesy of L. Flanagan).

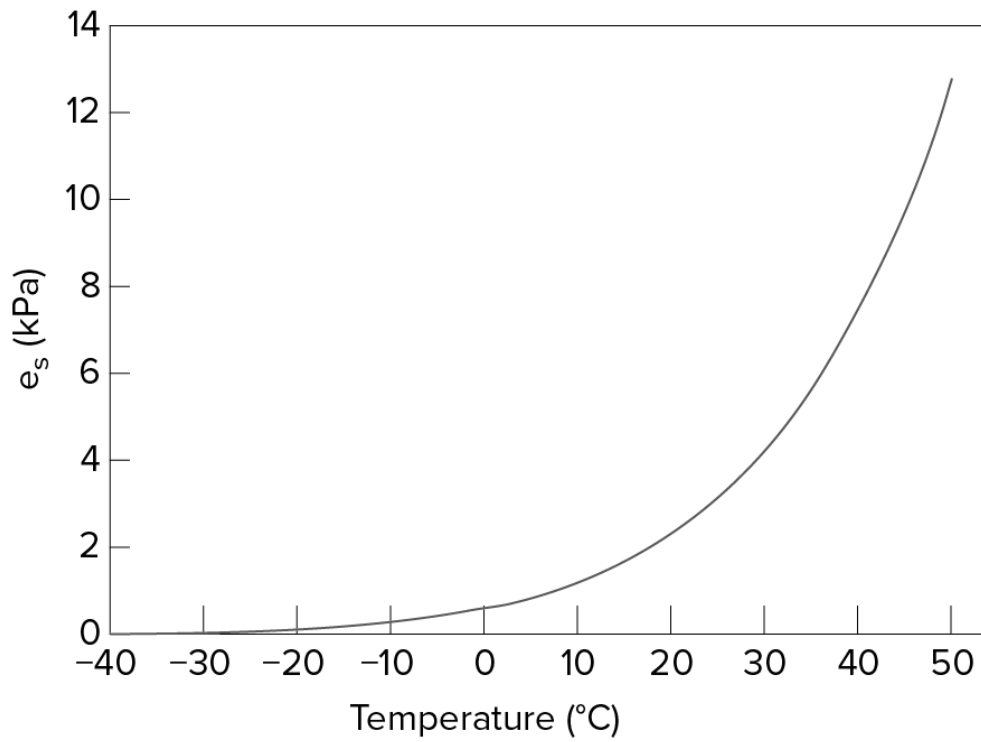


Figure 8: Curve giving equilibrium vapour pressure versus temperature. (Ross, Fig 7.4.)

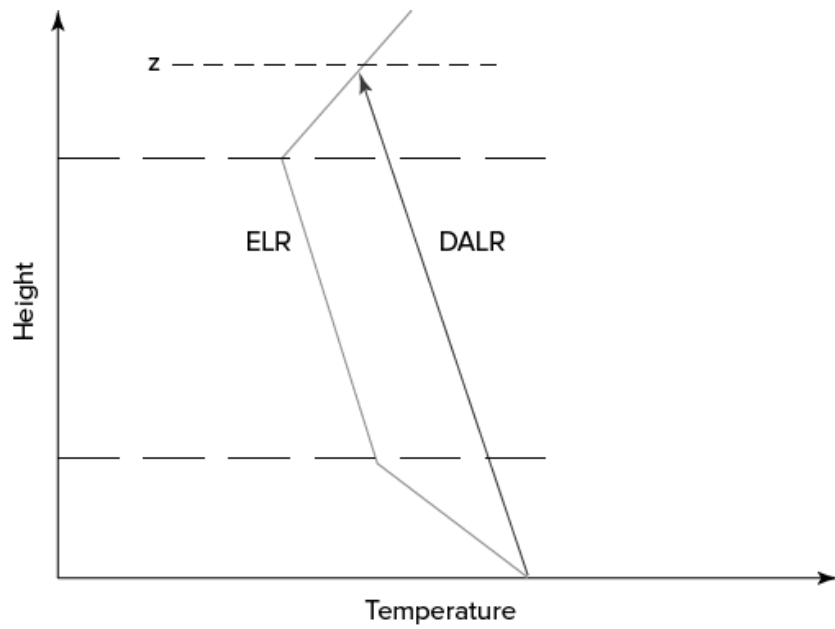


Figure 9: Idealized three-layer summer, daytime temperature profile. (Ross's Figure 8.21).

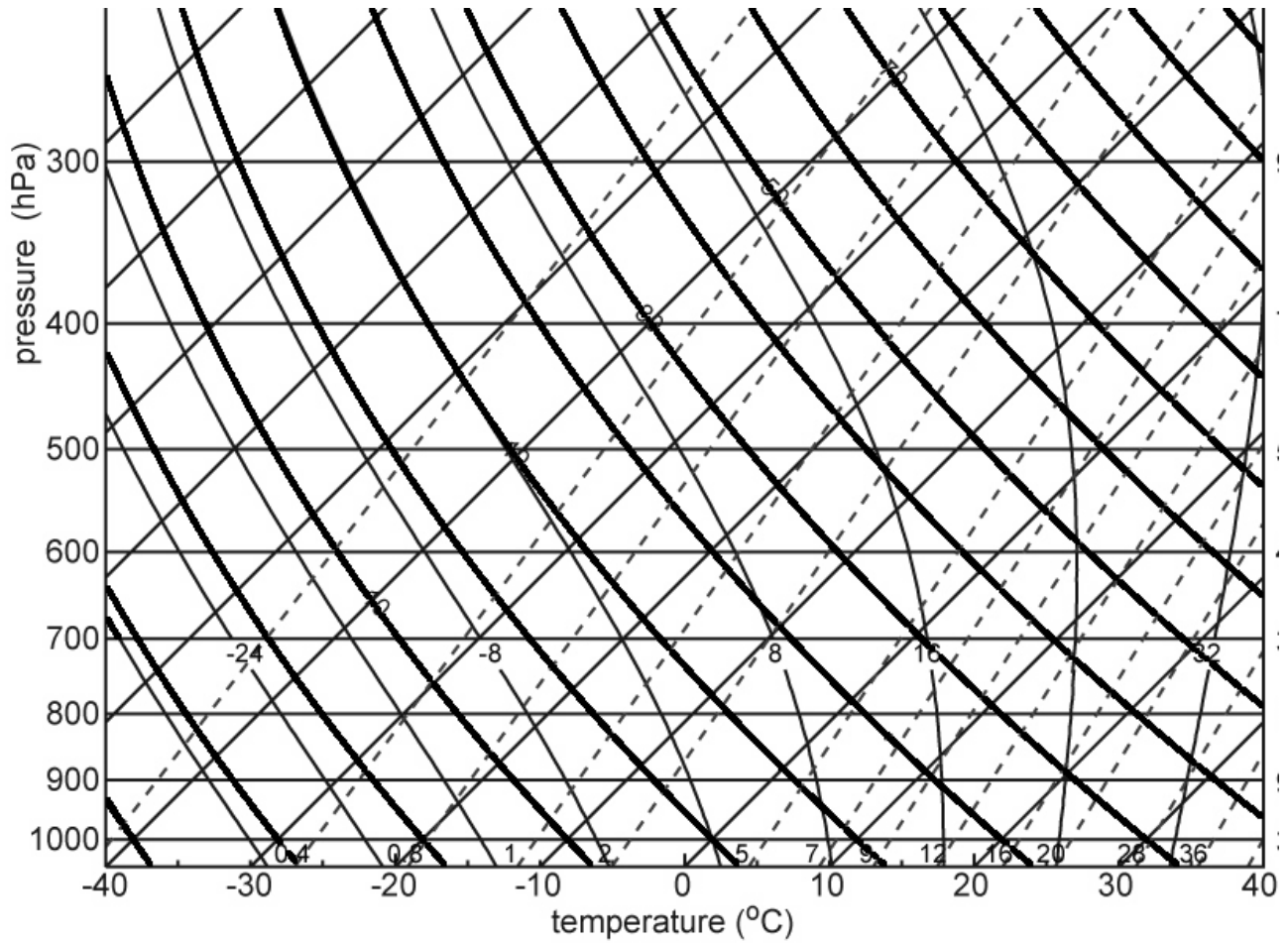


Figure 10: Blank skew-T/log-P diagram. Heavy solid curves are dry adiabats, lighter solid curves are moist adiabats, dashed lines are isohumes, and straight lines are isobars or isotherms..

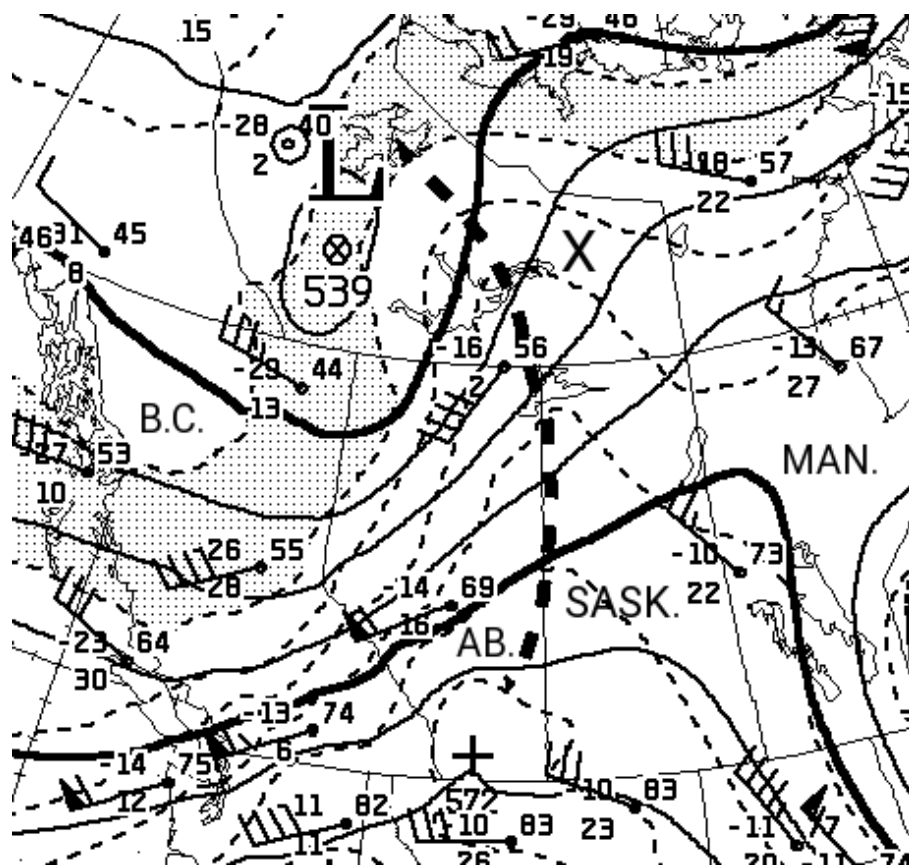


Figure 11: CMC 500 hPa analysis (cropped) for 12Z on 27 Sept. 2016. Secondary field is the 1000-500 hPa thickness, and the contour on the “warm side” of the stippled zone is the 540 dam thickness contour.

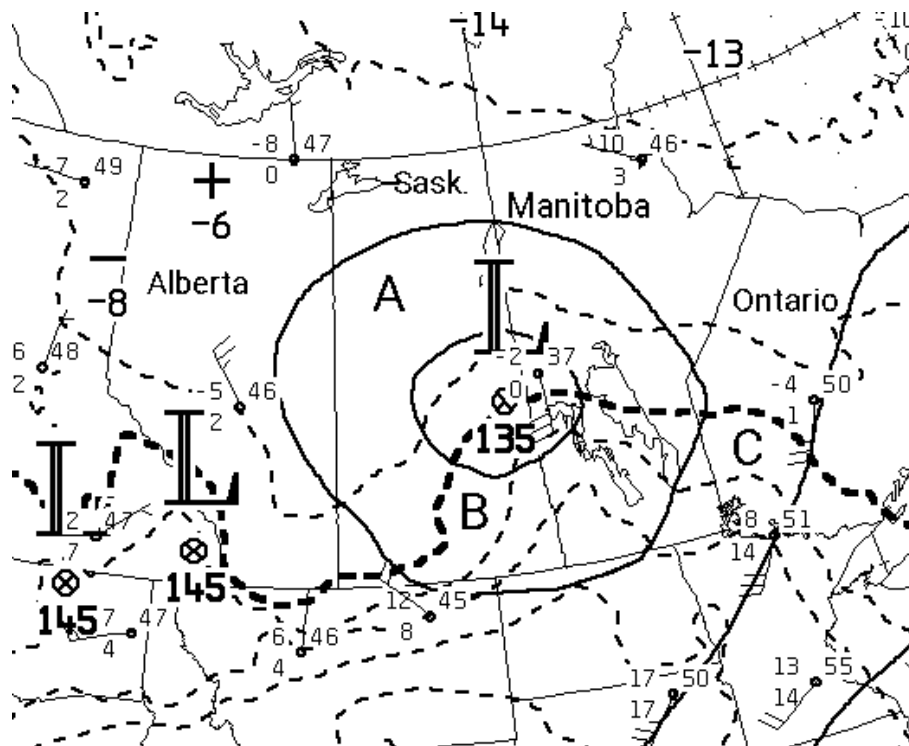


Figure 12: CMC 850 hPa analysis (cropped) for 00Z on 10 Oct. 2016.